

# Thesis Seminar

## Meta-analysis

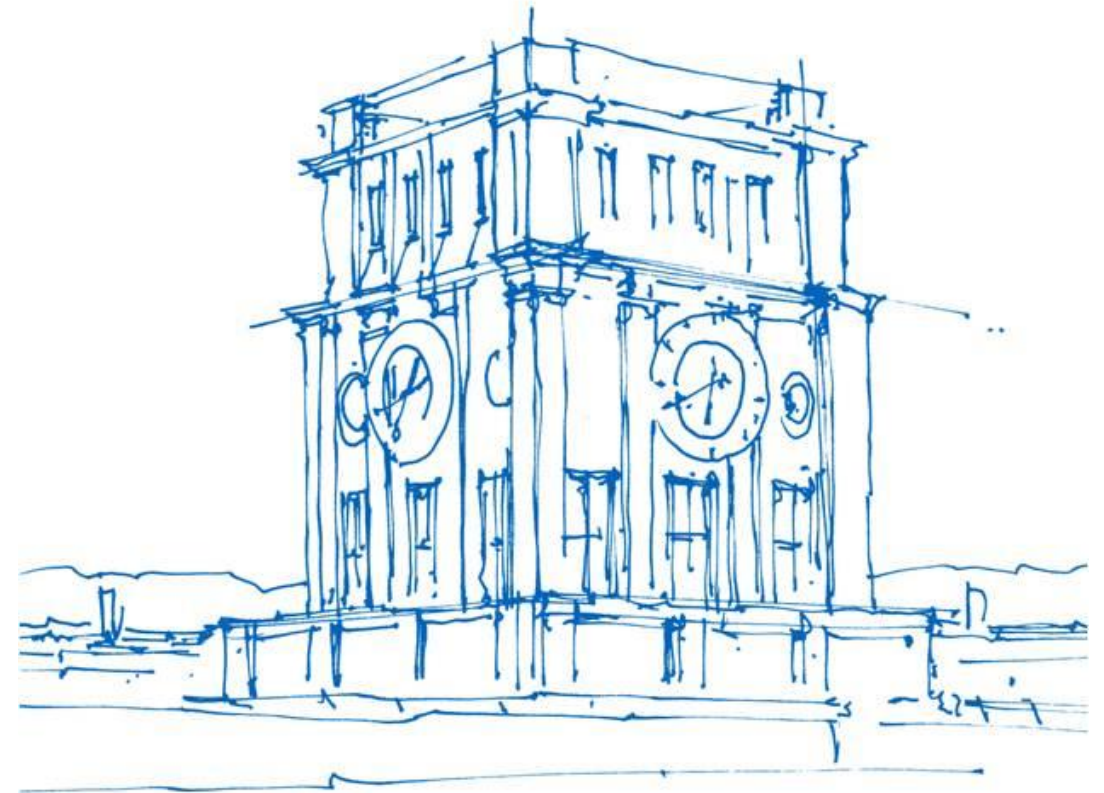
**Dr. Theresa Treffers**

Technical University of Munich

TUM School of Management

Chair for Strategy and Organization

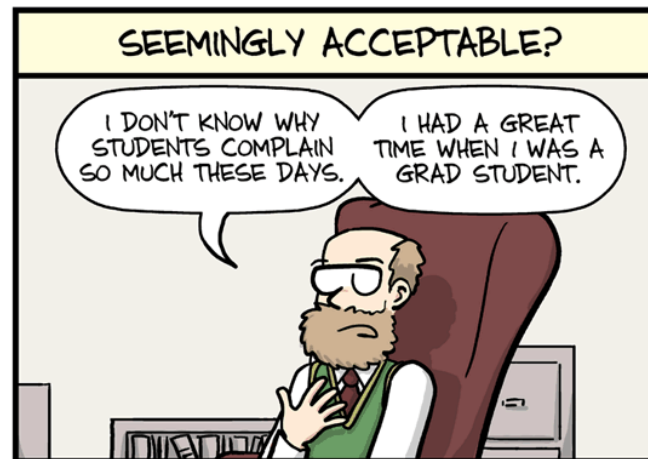
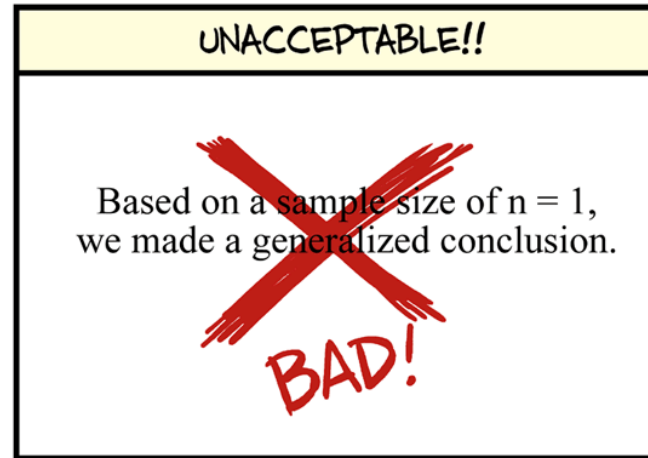
Prof. Dr. Isabell M. Welp



*Uhrenturm der TUM*

# Why do we need meta-analyses?

## ACADEMIC CONCLUSIONS



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# Why do we need meta-analyses?

- Nowadays an enormous stream of academic publications!
- A single study does not provide a precise, definite answer
- Science is cumulative: many studies are (partial) replications and extensions

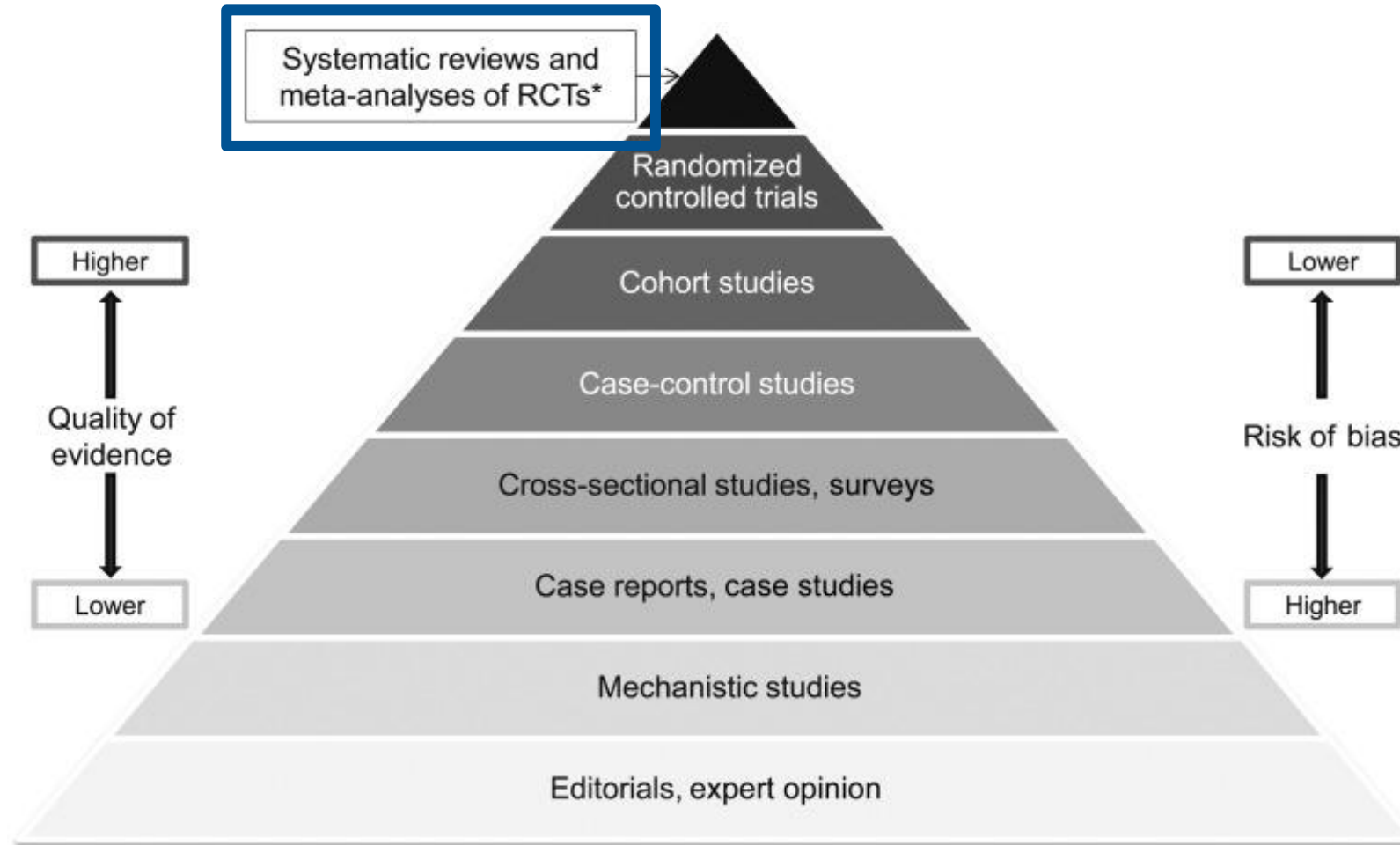
**But** do more and more empirical findings lead to **more certainty**

or to **more variety and inconsistency** in results...?

**Required:**

- Insightful **summary or overview**
- Combine a (large) set of studies to determine the **limits & conditions of findings**

# Meta-analysis on experiments: highest level of evidence



# Agenda



1. **What** are meta-analyses?
2. **How** are meta-analyses conducted?
3. How to **read & critically examine** meta-analytical findings?
4. **Best practices** & further readings

**What are meta-analyses?**

# What are meta-analyses?

“**The analysis of analyses.**”

- Gene V. Glass in “Primary, secondary and meta-analysis of research”, 1976.

## **Definition:**

= statistical integration of all “published” (better: existing) empirical research results through quantitative comparison & combining of these findings

Meta-analyses **overcome typical problems & validity issues of primary studies**

- For meta-analysis, effect sizes are summarized **independently of significance**
- Weighted, mean effect size over all studies is **closer to true effect** in the whole population

# How to conduct meta-analyses?



# Process of conducting a meta-analysis



1. Definition of the research proposition

2. Data collection

- a) Collection of studies
- b) Selection / Exclusion of studies
- c) Development of coding questionnaire
- d) Coding of studies

3. Data analysis

- a) Computation of effect sizes
- b) Dealing with publication bias
- c) Examination of heterogeneity
- d) Moderator analysis, meta-regression, ...

4. Report findings

5. Formulation of conclusions and directions for further research

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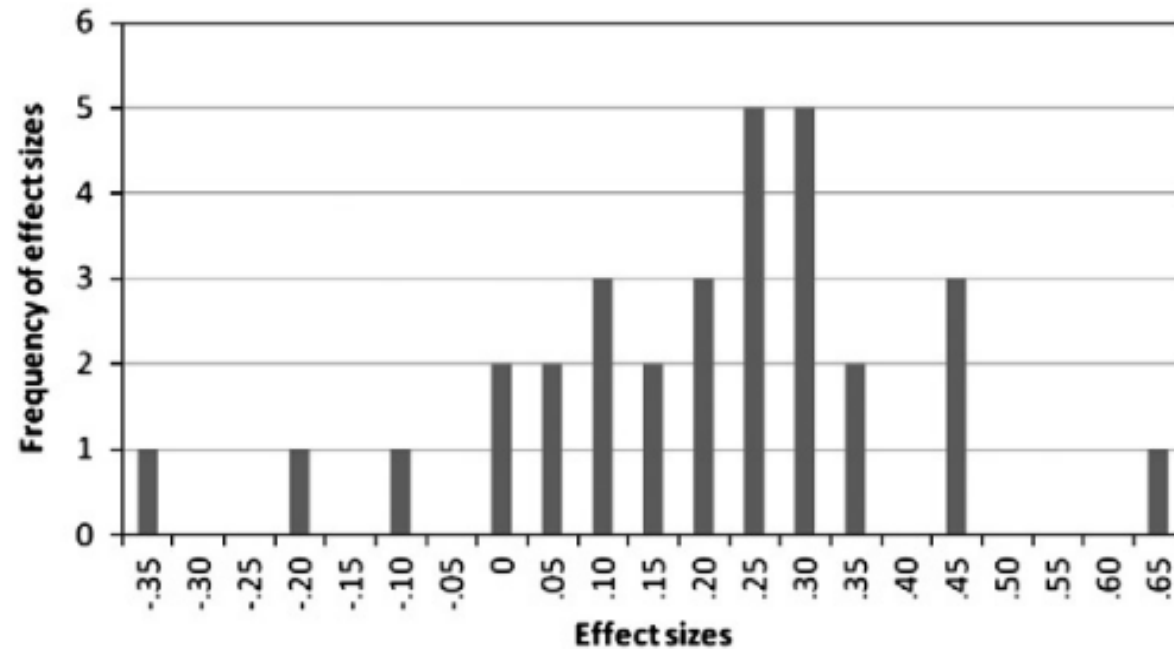
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# Example: Contradictory findings



**Fig. 1.** Range of effect sizes ( $r$ ) for the relationship between transformational leadership and innovation (aggregated correlations).

# But ...



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# Collection of studies

- Recommendation: **systematic literature review**
  - But meta-analyses do **not necessarily** require a comprehensive set of studies
- example: **single-study meta-analysis**

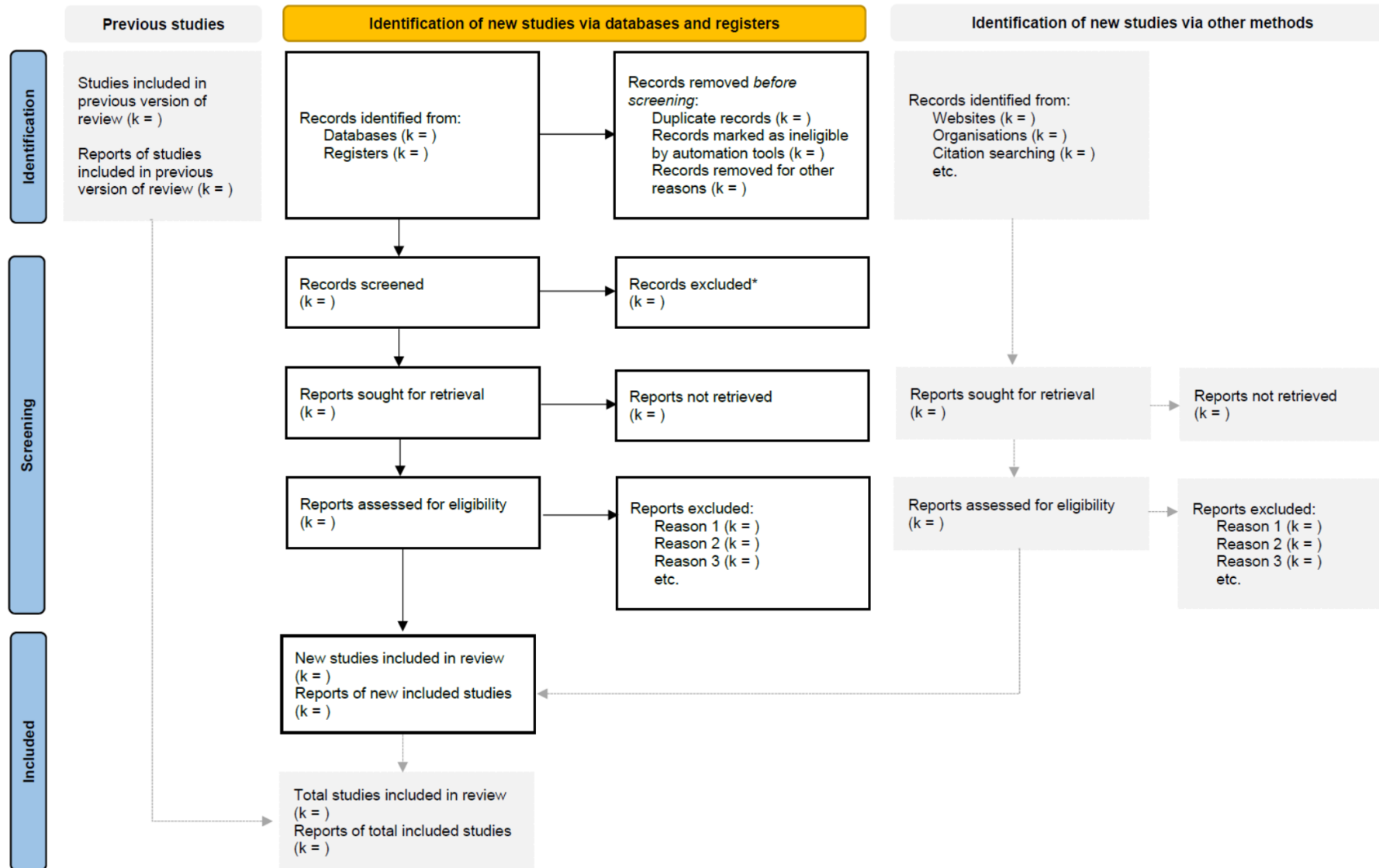
**TABLE 3** Meta-analysis of main effect sizes

	Integral							Incidental						
	<i>k</i>	<i>d</i>	95% CI	<i>p</i>	<i>Q</i>	<i>I</i> <sup>2</sup>	<i>T</i> <sup>2</sup>	<i>k</i>	<i>d</i>	95% CI	<i>p</i>	<i>Q</i>	<i>I</i> <sup>2</sup>	<i>T</i> <sup>2</sup>
<b>Anger</b>														
Deliberative RPs	14	0.17	0.06, 0.29	.003	20.07	35.23	0.03	14	-0.17	-0.28, -0.06	.003	34.46	68.28	0.07
Affective RPs	14	0.14	0.02, 0.25	.018	18.21	28.59	0.02	14	-0.07	-0.18, 0.04	.217	17.54	25.90	0.02
Experiential RPs	14	0.15	0.03, 0.26	.011	19.42	33.07	0.02	14	-0.10	-0.22, 0.01	.067	18.66	30.23	0.02
Intentions	10	-0.15	-0.27, -0.03	.014	31.11	71.07	0.10	10	-0.06	-0.18, 0.06	.324	4.69		
<b>Fear</b>														
Deliberative RPs	16	0.26	0.17, 0.36	<.001	21.22	29.30	0.02	16	-0.01	-0.10, 0.09	.910	9.17		
Affective RPs	16	0.31	0.22, 0.41	<.001	43.75	65.72	0.07	16	-0.01	-0.10, 0.08	.854	1.76		
Experiential RPs	16	0.28	0.18, 0.37	<.001	33.84	55.67	0.05	16	0.01	-0.08, 0.10	.820	9.81		
Intentions	12	-0.10	-0.20, -0.01	.036	35.67	69.16	0.07	12	-0.01	-0.10, 0.09	.957	22.54	33.45	0.02

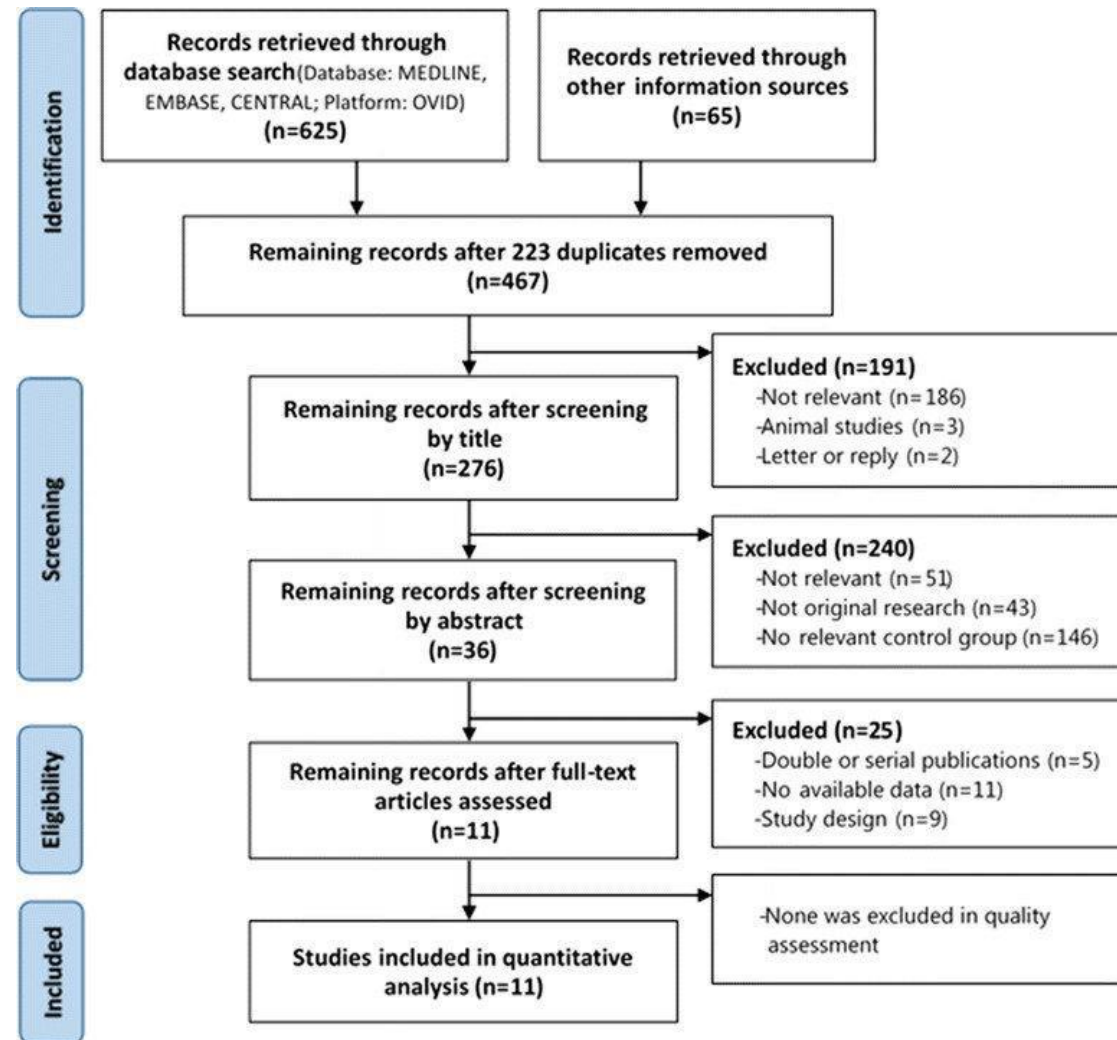
Note. *I*<sup>2</sup> and *T*<sup>2</sup> reported only with significant *Q*. Bolded values are significant at *p* < .05.

Abbreviations: CI, confidence interval; RP, risk perception.

# PRISMA Flow Chart



# PRISMA Flow Chart - Example





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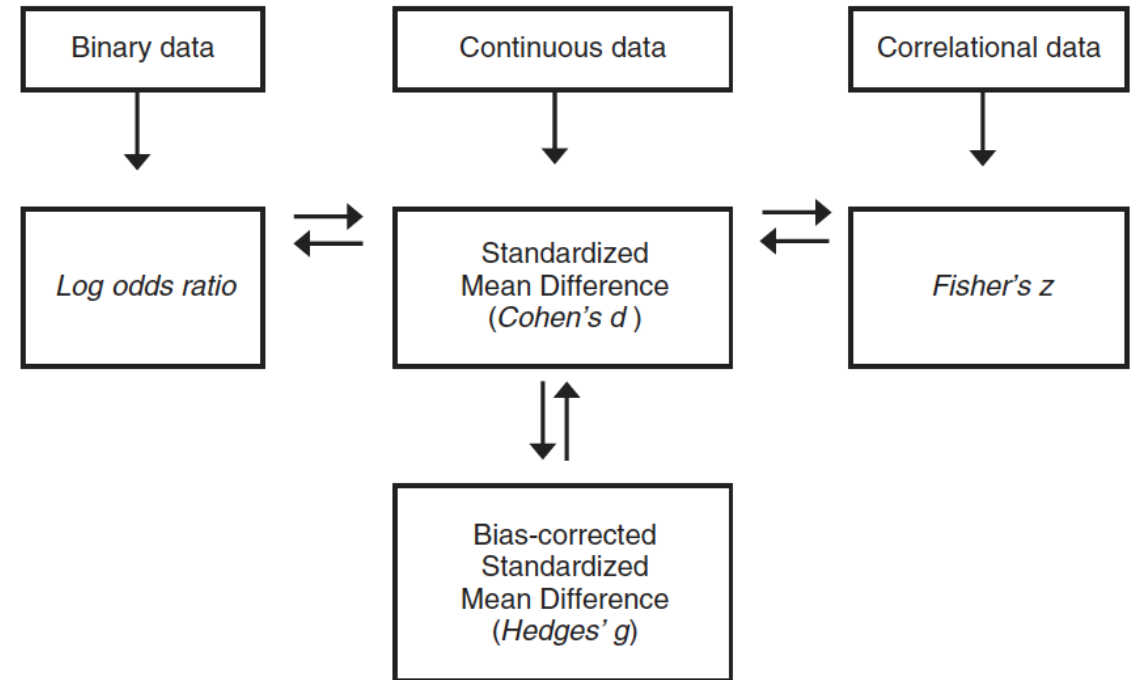
5. Formulation of conclusions and directions for further research

# Coding table

<b>A</b>	<b>B</b>		<b>D</b>	<b>E</b>		<b>G</b>	<b>H</b>	<b>I</b>	<b>J</b>
Stud_ID	Jahr	...	Samp_ID	N	...	ES_ID	aV	aV_Name	ES_r
01	1998	...	01	245	...	01	6	Job satisfaction	.26
01	1998	...	02	316	...	02	7_1	Emotional attachment	.34
01	1998	...	02	316	...	03	7_2	Turnover thoughts (rev.)	.32
01	1998	...	02	316	...	04	7	Comb: Org. attachment	.33
02	2005	...	03	81	...	05	7	Org. attachment	.4

# Choosing and calculating effect sizes

- Choice **based on reported studies**
- Effect sizes can be **converted** into others
- Most studies do not report effect sizes, hence **calculation is necessary**



**Often more than one effect size from one study** (different treatment groups, multiple comparisons etc.)  
→ Before calculation of summary effect: combining or correcting dependent effect sizes & standard errors

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# Computation of the summary effect: Fixed effect model vs. random effects model

## Fixed effect model:

- All studies included in analyses are **functionally identical**
- Goal: estimate **one true effect**
- **No generalization** to other populations

## Random effects model:

- Studies **not functionally identical**
  - Goal: estimate **mean of effects' distribution**
  - **Generalize** to other populations
- ⚠ Only applicable if enough studies available!

Impact of Intervention (Fixed effect)

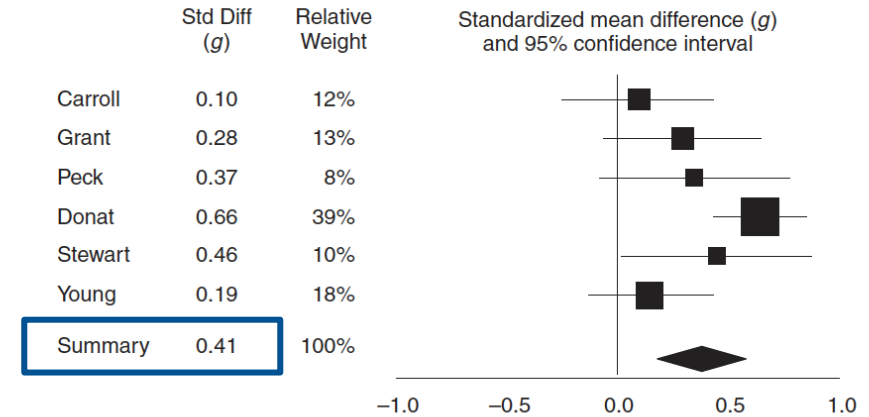


Figure 13.1 Fixed-effect model – forest plot showing relative weights.

Impact of Intervention (Random effects)

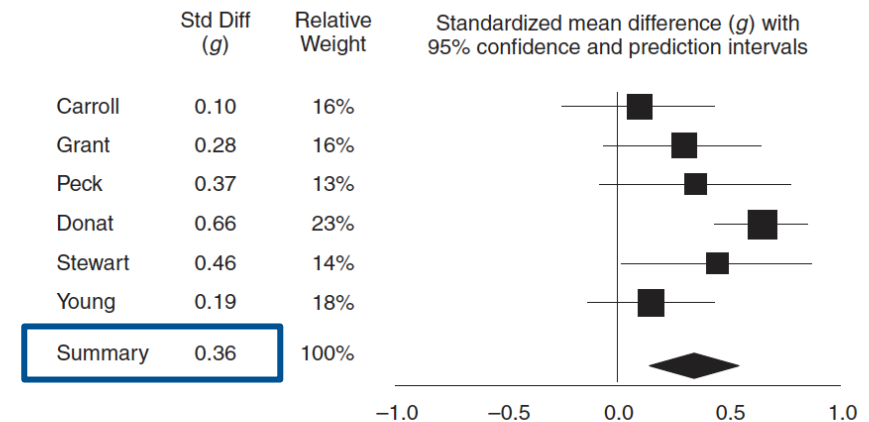


Figure 13.2 Random-effects model – forest plot showing relative weights.

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# The file drawer problem

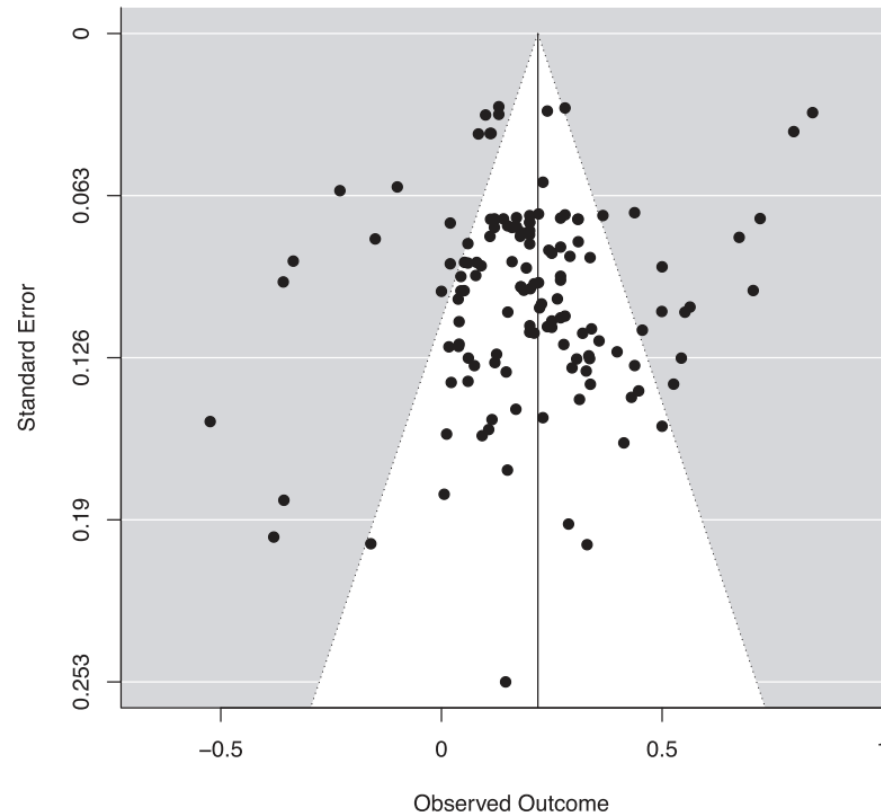
⚠ Studies with significant intervention effect tend to be **published more often** than studies with null results

## Tests: (exemplary)

- Funnel plot
- Orwin's Fail-Safe-N-Test

## Solutions: (exemplary)

- Search for grey literature
- Trim-and-Fill
- Cumulative meta-analysis



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# Assessing heterogeneity

**Heterogeneity** = variation in true effect sizes

Important because heterogeneity could suggest

- The existence of **outliers**
- The existence of **subgroups**
- That we **compare apples with oranges**

**Important estimators:** Q test,  $I^2$ ,  $T^2$

**Investigation via**

- Outlier detection with Confidence Intervals
- Influence Analysis
- Gosh Plot Analysis
- (4. Subgroup analyses)

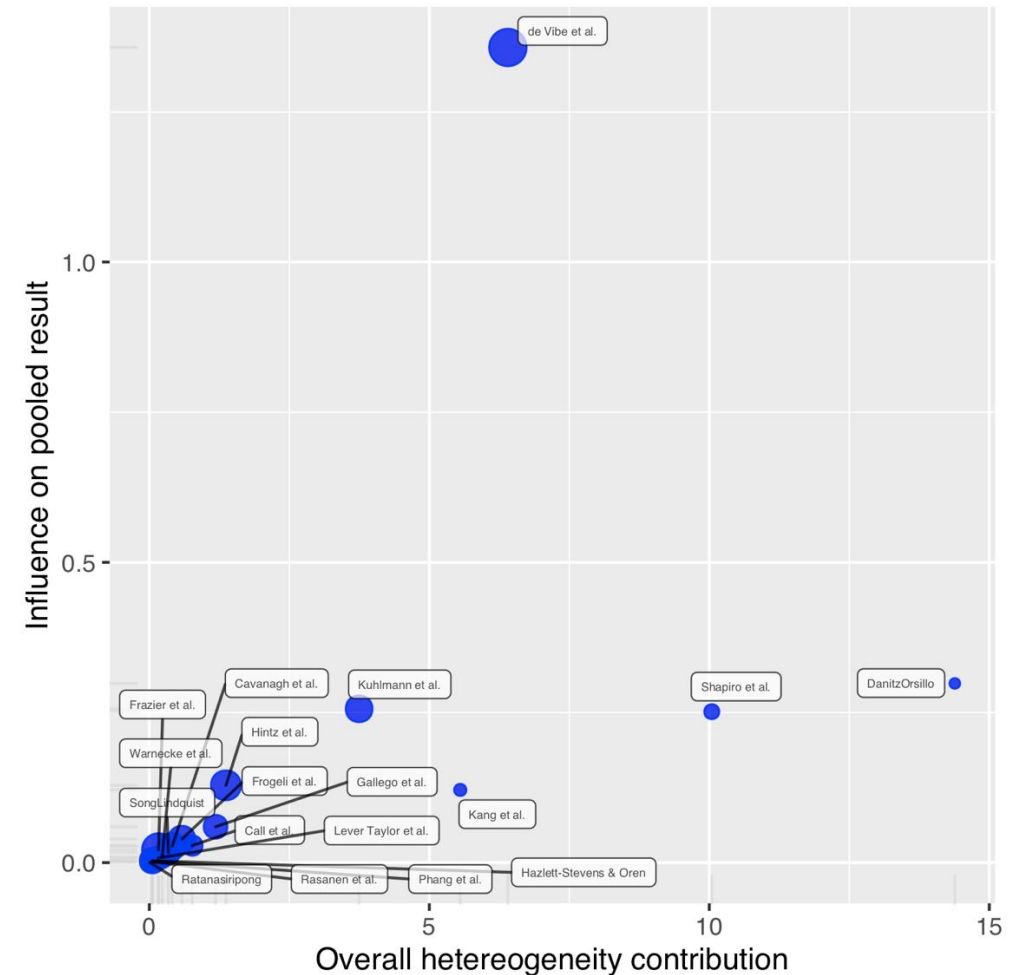


Figure 6.2: Baujat Plot

Borenstein, M., Hedges, L. V., Higgins, J. P., & Rothstein, H. R. (2021). *Introduction to meta-analysis*. John Wiley & Sons

Viechtbauer, W., & Cheung, M. W.-L. (2010). Outlier and influence diagnostics for meta-analysis. *Research Synthesis Methods*, 1(2), 112–125.

<https://doi.org/10.1002/jrsm.11>

Figure: Harrer, M., Cuijpers, P., Furukawa, T.A., & Ebert, D. D. (2019). *Doing Meta-Analysis in R: A Hands-on Guide*. DOI:

0.5281/zenodo.2551803.[https://bookdown.org/MathiasHarrer/Doing\\_Meta\\_Analysis\\_in\\_R/](https://bookdown.org/MathiasHarrer/Doing_Meta_Analysis_in_R/)

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# Moderator analyses

## Options

1. **Subgroup analyses**
2. **Correlations** between moderator & common effect size
3. **Meta-regression**

## Because of

- a. A priori hypotheses
- b. High heterogeneity

→ **Better:** specific set of moderators based on theoretical assumptions because of capitalization of chance

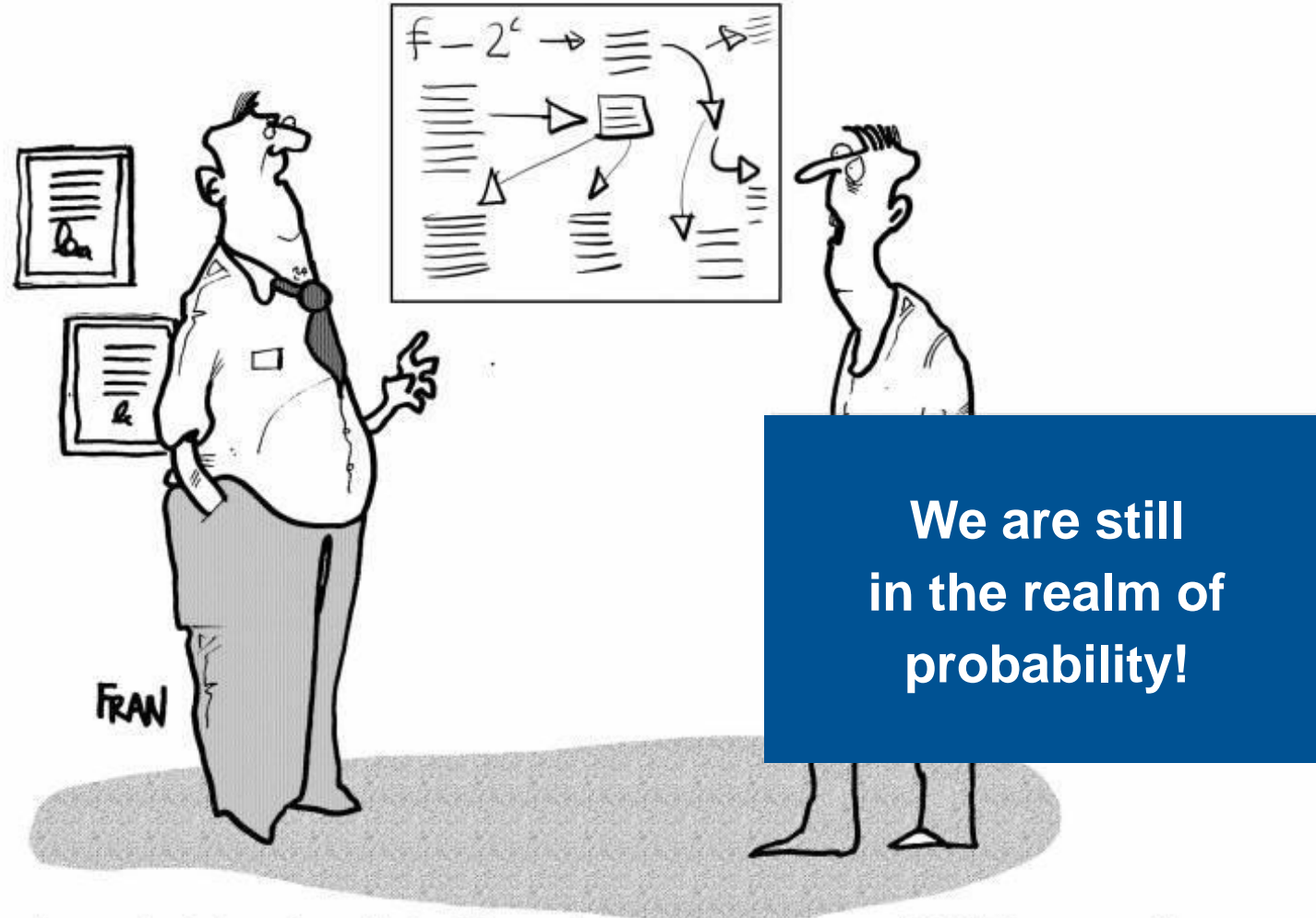
→ In subgroup analyses: watch out for **interdependence/correlation** of moderators

→ Meta-regression not advised as it is error-prone & requires high  $k$

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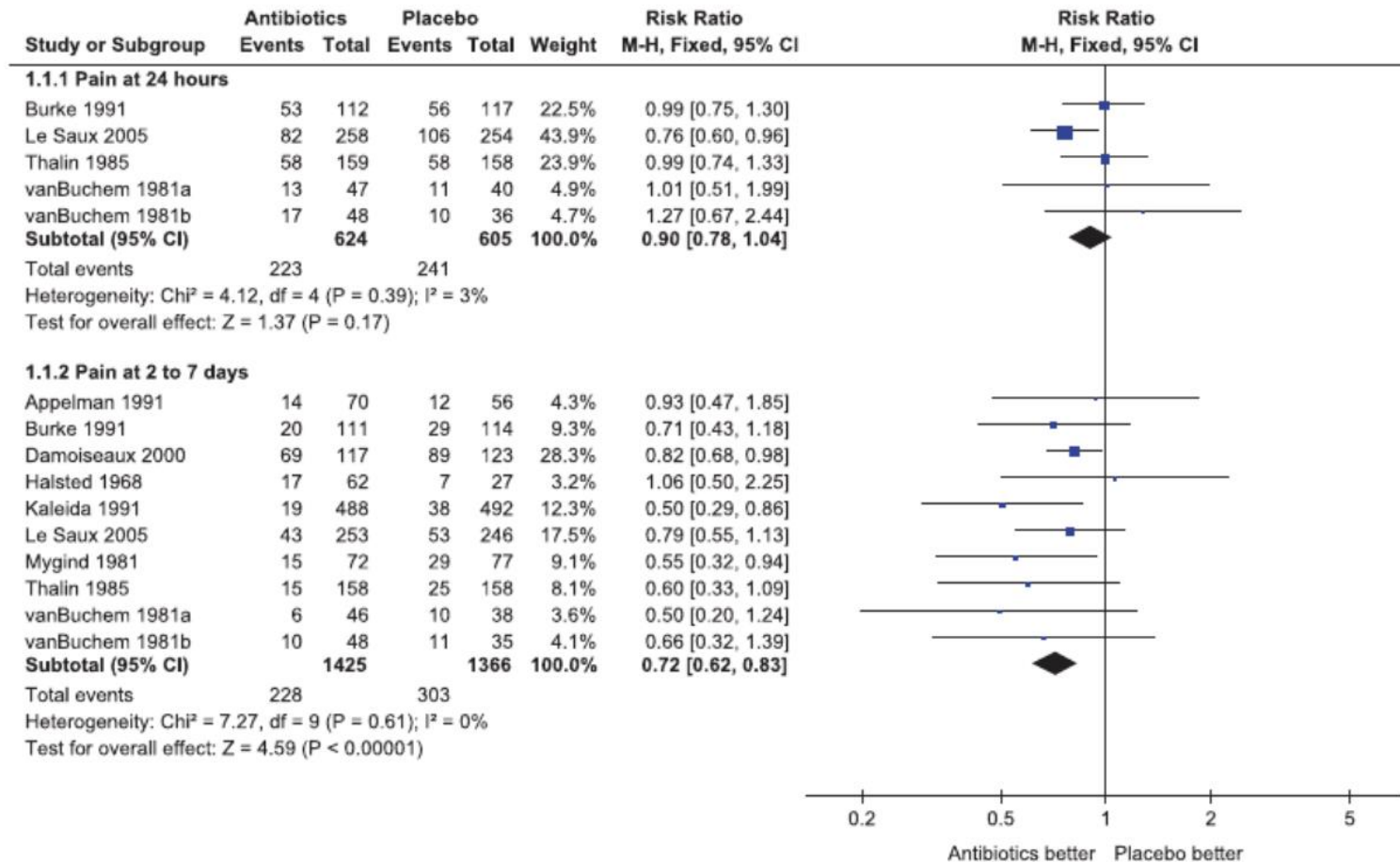
# How to read & critically examine meta-analytical findings?

# What is important when reading meta-analyses?



I've conducted a meta analysis of the myriad of tests we've run and I think I can say with a certain level of certainty that you are probably screwed...

# How to read a meta-analysis? - Forest Plot



**Figure 1.** Forest plot. Antibiotics for acute otitis media in children: Effect on recovery from pain [16]. Copyright Cochrane Collaboration, reproduced with permission.

# How to read a meta-analysis? - Table



Table 3. Overall results for treatment–control sample on judgement and decision-making outcomes by emotion group comparison

	<i>k</i>	<i>N</i>	<i>d</i>	<i>SD</i>	<i>SE</i>	<i>PVA</i>	95% CI		<i>Q</i>	
							<i>L</i>	<i>U</i>		
<i>TC<sup>j</sup></i>										
Anger	6	535	0.06	0.09	0.05	100.00	−0.04	0.16	1.16	
Fear	6	542	0.11*	0.11	0.05	100.00	0.01	0.21	1.54	
Sadness	9	553	0.18*	0.22	0.07	100.00	0.04	0.32	6.66	
Happiness	5	304	0.17*	0.26	0.07	100.00	0.03	0.31	4.83	
<i>TC<sup>dm</sup></i>										
Anger	10	862	0.26***	0.29	0.05	58.69	0.16	0.36	17.04*	
Fear	6	484	0.18***	0.19	0.05	100.00	0.08	0.28	4.44	
Sadness	13	975	0.33***	0.28	0.06	71.02	0.21	0.45	18.31	
Disgust	2	192	0.36***	0.27	0.04	59.06	0.28	0.44	3.39	
Guilt	3	333	0.98***	0.34	0.04	34.85	0.90	1.06	8.61*	

Notes:  $TC^j$  = treatment–control judgement sample;  $TC^{dm}$  = treatment–control decision-making sample; *k* = number of effect-size estimates; *N* = sum of participants; *d* = average sample-weighted effect-size estimate using Cohen's *d*; *SD* = standard deviation of effect-size estimates; *SE* = standard error of effect-size estimates; *PVA* = percent of variance accounted for by sampling error; 95% CI = 95% confidence interval; *Q* = *Q* statistic (Hunter & Schmidt, 1990). \**p* < .05; \*\**p* < .01; \*\*\**p* < .001.



# Example: Business Case for Women Leaders



**Table 2**  
**Meta-Analytic Results for Women's Representation in Leadership**  
**and Firm Financial Performance**

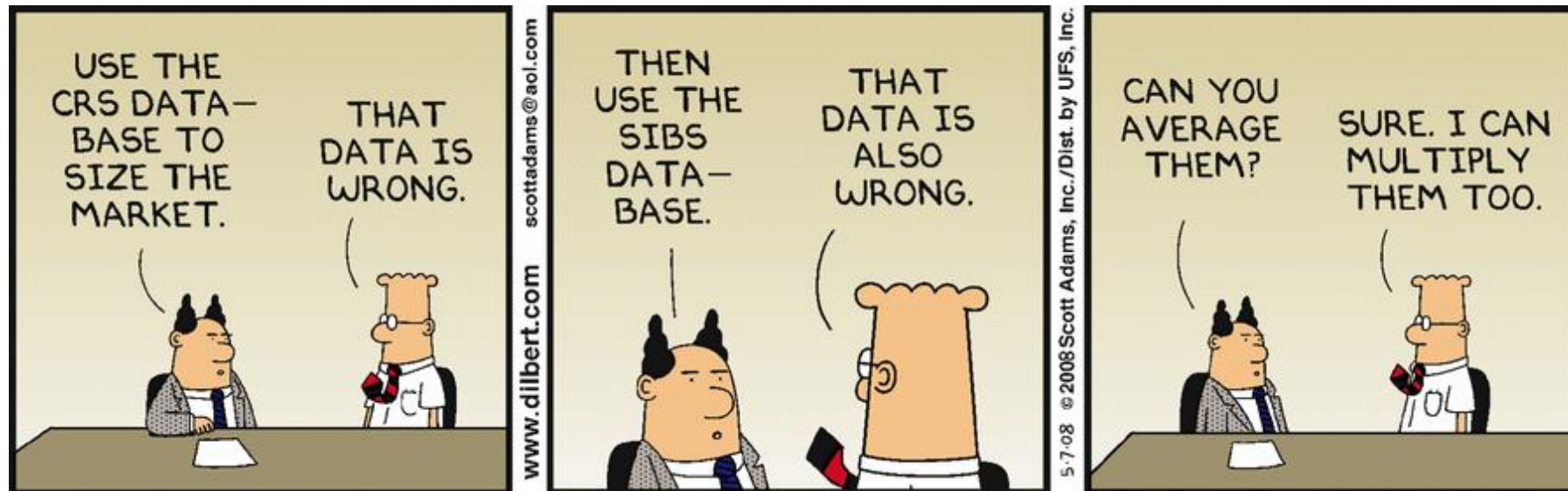
	<i>k</i>	<i>n</i>	$\bar{p}$	95% Confidence Interval	80% Credibility Interval	<i>Q<sub>w</sub></i>
Women's leadership and firm performance	78	117,639	+02	+01 to +04	-.07 to +.12	345.51*
Female representation on board of directors	62	75,978	+04	+05 to +09	-.04 to +.18	561.95*
Female CEO	12	45,165	-.02	-.04 to +.15	-.08 to +.05	-64.72
Female representation on top management team	13	27,431	+01	-.00 to +.04	-.03 to +.07	165.66*
Accounting performance measures	75	111,905	+02	+01 to +05	-.09 to +.15	246.03*
Return on assets	46	90,368	+03	-.00 to +.05	-.09 to +.13	150.16*
Return on equity	20	37,026	+05	-.03 to +.03	-.09 to +.09	-9.58
Leverage	18	56,119	+06	-.00 to +.05	-.11 to +.13	119.56*
Sales	10	18,077	+04	+03 to +.37	-.16 to +.56	25.84*
Profitability	9	4,329	+00	-.01 to +.14	-.08 to +.20	46.10*
Composite measure	5	1,041	-.05	-.09 to +.04	-.12 to +.09	-22.90
Return on capital	3	205	-.03	-.20 to +.24	-.33 to +.35	-1.33
Return on investment	2	850	+01	-.05 to +.06	-.04 to +.07	8.67*
Market performance measures	30	67,627	+05	+01 to +05	-.05 to +.10	228.93*
Tobin's <i>Q</i>	17	56,348	+01	-.00 to +.06	-.06 to +.12	115.93*
Stock performance	14	21,011	+06	-.06 to +.04	-.14 to +.12	-14.65
Market capitalization	4	3,879	+14	-.08 to +.16	-.12 to +.20	10.61*

*Note:* Confidence intervals in italics include 0; credibility intervals in italics range in excess of .11. *k* = number of effect sizes;  $\bar{p}$  = mean estimate of the Fisher's *z*-transformed corrected population correlation of the cumulated effect sizes.

\**p* < .05.



# Always keep in mind ...



... garbage in, garbage out!

# Best practices & further readings

# 5 Things to Know About Meta-Analysis

1. A meta-analysis is a **safer starting point than a single study**  
– but it won't *necessarily* be more reliable
2. A meta-analysis is a **snapshot in time**  
– it can even be out-of-date the day it's published
3. **Look carefully** before you take an outcome literally  
– it may not be what it appears to be
4. **Data choices and statistical technique** can change a result
5. **Absence of evidence** is not evidence of absence  
...most of the time

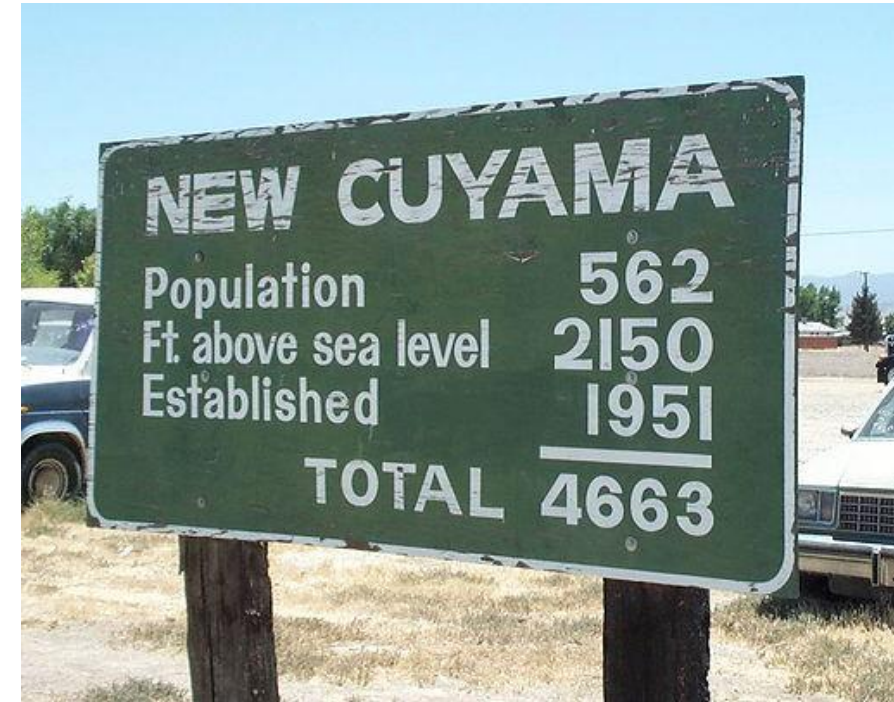


Photo by Mike Gogulski (Wikimedia Commons)

# Additional materials:

## Tutorial videos on meta analysis

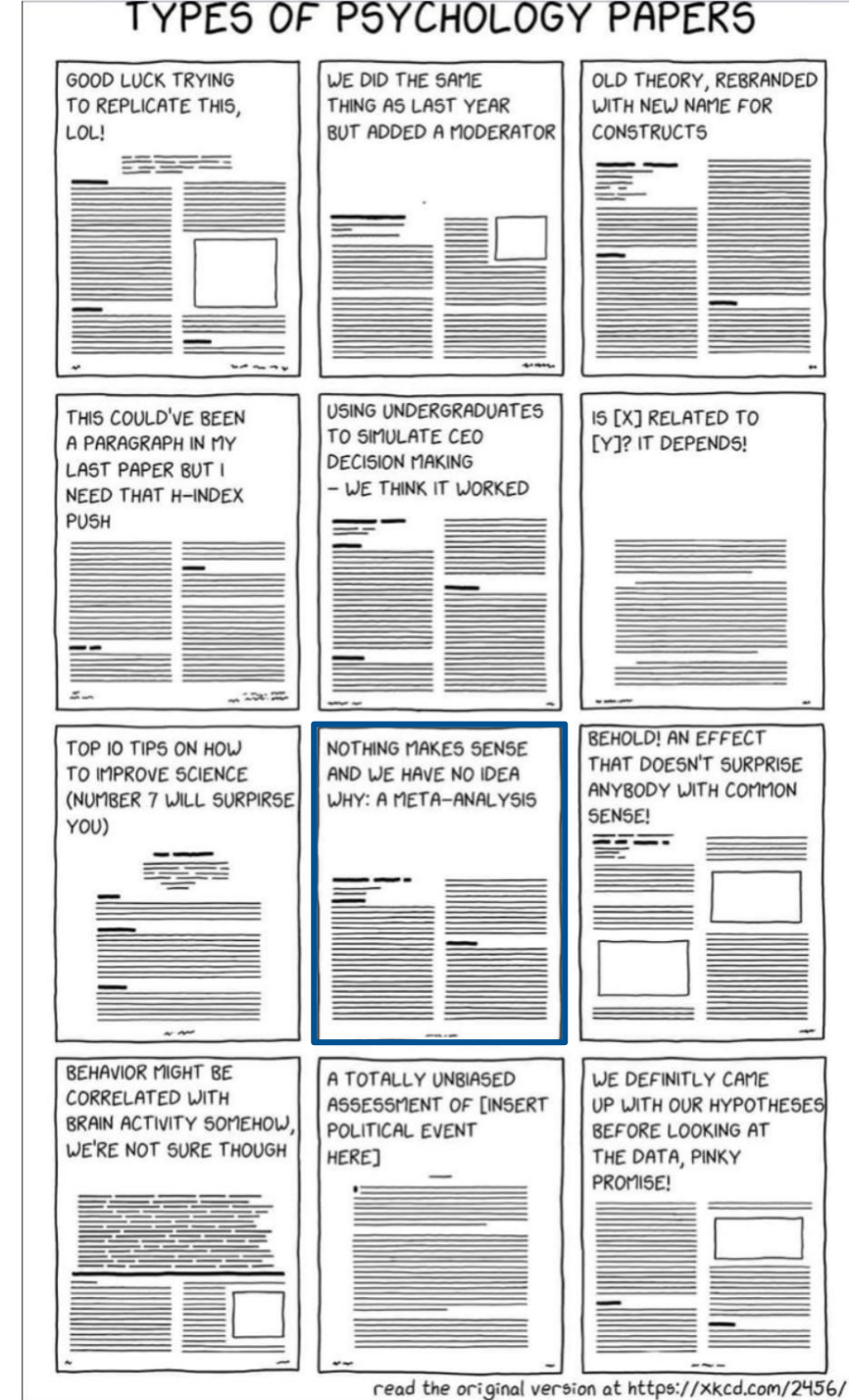
<http://metalab.stanford.edu/tutorials.html>

The website offers several video tutorials on the following questions:

- Why meta-analysis (MA)?
- What are effect sizes?
- How do I define my MA question?
- Why should I bother keeping track of the MA creation process?
- Now that I have my list of related studies, how do I set my inclusion criteria?
- How do I select the studies to include?
- How exactly can I go about looking through my initial list and making decisions?
- What are the relevant variables for a MA, and how many input rows/columns should I make?
- How do I enter and code relevant studies?
- How do I calculate Effect Sizes?
- What if I don't have all the required information?
- How to run a meta-analytic regression ?
- Are there some MA specific plots that I should make?

# Own experiences/Best practices

- Published meta-analyses often do not stick to guidelines
- Learning by doing
- Document each step
- Report for replicability
- Be critical about own results
- Use R packages or other software for calculations





## Recommended books

- Borenstein, M., Hedges, L. V., Higgins, J. P., & Rothstein, H. R. (2021). *Introduction to meta-analysis*. John Wiley & Sons → My favorite!
- Schmidt, F. L., & Hunter, J. E. (2003). Meta-analysis. *Handbook of psychology*, 533-554.
- Lipsey, M. W., & Wilson, D. B. (2001). *Practical meta-analysis*. SAGE publications, Inc. → especially for how to calculate effect sizes from missing data

## Useful guides for conducting meta-analyses with R

- Harrer, M., Cuijpers, P., Furukawa, T.A, & Ebert, D. D. (2019). *Doing Meta-Analysis in R: A Hands-on Guide*. DOI: 10.5281/zenodo.2551803. [https://bookdown.org/MathiasHarrer/Doing\\_Meta\\_Analysis\\_in\\_R/](https://bookdown.org/MathiasHarrer/Doing_Meta_Analysis_in_R/)
- Viechtbauer, W. (2010). Conducting meta-analyses in R with the metafor package. *Journal of Statistical Software*, 36(3), 1–48. <http://www.metafor-project.org/doku.php/>

# Questions?

